

Due Tuesday, November 16, 2021. Write all complex numbers and polynomials in standard form.

**Definition 1.** Let  $f$  be a polynomial and let  $a$  be a number. The *multiplicity* of  $a$  as a zero of  $f$  is the largest  $n$  such that  $(x - a)^n$  divides  $f$ .

**Problem 1.** Consider the polynomial  $f(x) = (x - 1)(x + 7)^2(x - 2)^3(3x - 2)(x + 8)$ . Find the multiplicity the following numbers.

Number	1	2	7	-7	3/2	2/3
Multiplicity						

**Problem 2.** Respond to the following prompts.

(a) Find two numbers whose product is 30 and whose sum is 11.

(b) Factor  $x^2 - 11x + 30$ .

(c) Find two numbers whose product is 30 and whose difference is 7.

(d) Factor  $x^2 - 7x - 30$ .

**Problem 3.** Solve the following quadratic equations. Correctly write the solution set.

(a)  $x^2 - 25 = 0$

(d)  $x^2 - 10x - 24 = 0$

(b)  $x^2 - 10x + 25 = 0$

(e)  $x^2 + 10x - 39 = 0$

(c)  $x^2 - 10x + 21 = 0$

(f)  $x^2 - 10x + 29 = 0$

**Problem 4.** Let  $f(x) = 3x^2 - 17x + 10$ . Suppose that  $f(x)$  factors as  $f(x) = (3x + p)(x + q)$ . Find  $p$  and  $q$ .

**Problem 5.** Let  $f(x) = x^3 - x^2 - 4x + 4$ . Use the technique we called “Factor by Grouping” to completely factor  $f$ .

**Problem 6.** Let  $f(x) = x^3 - 9x$ . Factor  $f$  to find its zeros. Find the  $x$ - and  $y$ - intercepts of  $f$ . Sketch the graph of  $f$ .